### **Binomial Expansion Exam Questions (from OCR 4722)**

### Q1, (Jan 2011, Q1)

- (i) Find and simplify the first three terms, in ascending powers of x, in the binomial expansion of  $(1+2x)^7$ . [3]
- (ii) Hence find the coefficient of  $x^2$  in the expansion of  $(2-5x)(1+2x)^7$ . [3]

### Q2, (Jan 2010, Q3)

- (i) Find and simplify the first four terms in the expansion of  $(2-x)^7$  in ascending powers of x. [4]
- (ii) Hence find the coefficient of  $w^6$  in the expansion of  $\left(2 \frac{1}{4}w^2\right)^7$ . [2]

### Q3, (Jun 2010, Q3)

- (i) Find and simplify the first four terms in the binomial expansion of  $(1 + \frac{1}{2}x)^{10}$  in ascending powers of x.
- (ii) Hence find the coefficient of  $x^3$  in the expansion of  $(3 + 4x + 2x^2)(1 + \frac{1}{2}x)^{10}$ . [3]

## Q4 (Jan 2009, Q7)

In the binomial expansion of  $(k + ax)^4$  the coefficient of  $x^2$  is 24.

- (i) Given that a and k are both positive, show that ak = 2. [3]
- (ii) Given also that the coefficient of x in the expansion is 128, find the values of a and k. [4]
- (iii) Hence find the coefficient of  $x^3$  in the expansion. [2]

#### Q5, (Jan 2013, Q4)

- (i) Find the binomial expansion of  $(2+x)^5$ , simplifying the terms. [4]
- (ii) Hence find the coefficient of  $y^3$  in the expansion of  $(2 + 3y + y^2)^5$ . [3]

#### Q6, (Jun 2013, Q3)

- (i) Find and simplify the first three terms in the expansion of  $(2 + 5x)^6$  in ascending powers of x. [4]
- (ii) In the expansion of  $(3 + cx)^2(2 + 5x)^6$ , the coefficient of x is 4416. Find the value of c. [3]

### Q7, (Jun 2014, Q6)

- (i) Find the binomial expansion of  $\left(x^3 + \frac{2}{x^2}\right)^4$ , simplifying the terms. [5]
- (ii) Hence find  $\int \left(x^3 + \frac{2}{x^2}\right)^4 dx$ . [4]

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# Q8 (Jun 2015, Q4)

(i) Find and simplify the first three terms in the binomial expansion of  $(2 + ax)^6$  in ascending powers of x.

[4]

[3]

(ii) In the expansion of  $(3-5x)(2+ax)^6$ , the coefficient of x is 64. Find the value of a.

# Q9, (Jun 2016, Q3)

(i) Find the binomial expansion of  $(3 + kx)^3$ , simplifying the terms.

[4]

(ii) It is given that, in the expansion of  $(3 + kx)^3$ , the coefficient of  $x^2$  is equal to the constant term. Find the possible values of k, giving your answers in an exact form. [2]

# Q10, (Jan 2008, Q10)

(i) Find the binomial expansion of  $(2x + 5)^4$ , simplifying the terms.

[4]

(ii) Hence show that  $(2x+5)^4 - (2x-5)^4$  can be written as

$$320x^3 + kx$$

where the value of the constant k is to be stated.

[2]

(iii) Verify that x = 2 is a root of the equation

$$(2x+5)^4 - (2x-5)^4 = 3680x - 800,$$

and find the other possible values of x.

[6]