

Normal Approximations to the Binomial Distribution (OCR Exam Board Only)

1. For a normal distribution, state the amount of area that must lie within
 - a. 1 standard deviation of the mean [1]
 - b. 2 standard deviations of the mean [1]
 - c. 3 standard deviations of the mean. [1]

2. A discrete random variable X has the distribution $B(200, 0.2)$.
 - a. Show that this distribution can be modelled approximately by a normal distribution, stating the mean and variance of this normal distribution. [4]
 - b. Using this approximation, estimate the symmetrical interval (with the mean at its centre) in which $\frac{2}{3}$ of the total probability in the original model lies. [3]

3. A fair dice is thrown 90 times and it is classed as a "win" each time a six is thrown.
 - a. State the distribution that can be used to model this game (including the values of any parameters) and the make clear the assumptions required for this model to be valid. [3]
 - b. State the conditions for the distribution identified in (a) to be approximated by a normal distribution and show that these conditions are fulfilled. State the values of the parameters used in the normal approximation to the distribution in (a). [3]
 - c. Using the normal approximation identified in (b), find the value of k such that the probability that the number of sixes rolled is greater than k is equal to 0.025. [3]