

**Mixed Sequences Exam Questions (from OCR 4722)**

**Jun 2006**

- 6 (i)** John aims to pay a certain amount of money each month into a pension fund. He plans to pay £100 in the first month, and then to increase the amount paid by £5 each month, i.e. paying £105 in the second month, £110 in the third month, etc.

If John continues making payments according to this plan for 240 months, calculate

- (a)** how much he will pay in the final month, [2]  
**(b)** how much he will pay altogether over the whole period. [2]

- (ii)** Rachel also plans to pay money monthly into a pension fund over a period of 240 months, starting with £100 in the first month. Her monthly payments will form a geometric progression, and she will pay £1500 in the final month.

Calculate how much Rachel will pay altogether over the whole period. [5]

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**Jun 2007**

- 7 (a)** In an arithmetic progression, the first term is 12 and the sum of the first 70 terms is 12 915. Find the common difference. [4]  
**(b)** In a geometric progression, the second term is  $-4$  and the sum to infinity is 9. Find the common ratio. [7]
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**Jun 2008**

**10** Jamie is training for a triathlon, which involves swimming, running and cycling.

- On Day 1, he swims 2 km and then swims the same distance on each subsequent day.
- On Day 1, he runs 2 km and, on each subsequent day, he runs 0.5 km further than on the previous day. (Thus he runs 2.5 km on Day 2, 3 km on Day 3, and so on.)
- On Day 1 he cycles 2 km and, on each subsequent day, he cycles a distance 10% further than on the previous day.

- (i)** Find how far Jamie runs on Day 15. [2]  
**(ii)** Verify that the distance cycled in a day first exceeds 12 km on Day 20. [3]  
**(iii)** Find the day on which the total distance cycled, up to and including that day, first exceeds 200 km. [4]  
**(iv)** Find the total distance travelled, by swimming, running and cycling, up to and including Day 30. [4]
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**Jun 2010**

**4** A sequence  $u_1, u_2, u_3, \dots$  is defined by  $u_n = 5n + 1$ .

(i) State the values of  $u_1, u_2$  and  $u_3$ . [1]

(ii) Evaluate  $\sum_{n=1}^{40} u_n$ . [3]

Another sequence  $w_1, w_2, w_3, \dots$  is defined by  $w_1 = 2$  and  $w_{n+1} = 5w_n + 1$ .

(iii) Find the value of  $p$  such that  $u_p = w_3$ . [3]

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**9** A geometric progression has first term  $a$  and common ratio  $r$ , and the terms are all different. The first, second and fourth terms of the geometric progression form the first three terms of an arithmetic progression.

(i) Show that  $r^3 - 2r + 1 = 0$ . [3]

(ii) Given that the geometric progression converges, find the exact value of  $r$ . [5]

(iii) Given also that the sum to infinity of this geometric progression is  $3 + \sqrt{5}$ , find the value of the integer  $a$ . [4]

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**Jan 2012**

**6** A sequence  $u_1, u_2, u_3, \dots$  is defined by  $u_n = 85 - 5n$  for  $n \geq 1$ .

(i) Write down the values of  $u_1, u_2$  and  $u_3$ . [2]

(ii) Find  $\sum_{n=1}^{20} u_n$ . [3]

(iii) Given that  $u_1, u_5$  and  $u_p$  are, respectively, the first, second and third terms of a geometric progression, find the value of  $p$ . [4]

(iv) Find the sum to infinity of the geometric progression in part (iii). [2]

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**Jan 2013**

**6** (i) The first three terms of an arithmetic progression are  $2x, x + 4$  and  $2x - 7$  respectively. Find the value of  $x$ . [3]

(ii) The first three terms of another sequence are also  $2x, x + 4$  and  $2x - 7$  respectively.

(a) Verify that when  $x = 8$  the terms form a geometric progression and find the sum to infinity in this case. [4]

(b) Find the other possible value of  $x$  that also gives a geometric progression. [4]

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**Jun 2013**

- 6 Sarah is carrying out a series of experiments which involve using increasing amounts of a chemical. In the first experiment she uses 6 g of the chemical and in the second experiment she uses 7.8 g of the chemical.
- (i) Given that the amounts of the chemical used form an arithmetic progression, find the total amount of chemical used in the first 30 experiments. [3]
- (ii) Instead it is given that the amounts of the chemical used form a geometric progression. Sarah has a total of 1800 g of the chemical available. Show that  $N$ , the greatest number of experiments possible, satisfies the inequality

$$1.3^N \leq 91,$$

and use logarithms to calculate the value of  $N$ .

[6]

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