

Forces and Motion in 3 Dimensions (From OCR 4761)

Q1, (Jan 2005, Q3)

(i)	$\begin{pmatrix} x \\ -7 \\ z \end{pmatrix} + \begin{pmatrix} 4 \\ y \\ -5 \end{pmatrix} + \begin{pmatrix} 5 \\ 4 \\ -7 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$ <p>Equating components gives $x = -9, y = 3, z = 12$</p>	<p>M1</p> <p>A1 A1 A1</p>	<p>[Allow SC 2/4 if 9, -3, -12 obtained]</p>	4
(ii)	<p>We need $\sqrt{5^2 + 4^2 + (-7)^2}$ $= \sqrt{90}$ or 9.48683... so 9.49 (3 s. f.)</p>	<p>M1</p> <p>A1</p>	<p>Any reasonable accuracy</p>	2
total		6		

Q2, (Jan 2008, Q4)

(i)	<p>Resultant is $\begin{pmatrix} 4 \\ 1 \\ 2 \end{pmatrix} + \begin{pmatrix} -6 \\ 2 \\ 4 \end{pmatrix} = \begin{pmatrix} -2 \\ 3 \\ 6 \end{pmatrix}$</p> <p>Magnitude is $\sqrt{(-2)^2 + 3^2 + 6^2} = \sqrt{49} = 7 \text{ N}$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>F1</p>	<p>Adding the vectors. Condone spurious notation.</p> <p>Vector must be in proper form (penalise only once in the paper). Accept clear components.</p> <p>Pythagoras on their 3 component vector. Allow e.g. -2^2 for $(-2)^2$ even if evaluated as -4.</p> <p>FT their resultant.</p>	4
(ii)	<p>$\mathbf{F} + 2\mathbf{G} + \mathbf{H} = \mathbf{0}$</p> <p>So $\mathbf{H} = -2\mathbf{G} - \mathbf{F} = -\begin{pmatrix} -12 \\ 4 \\ 8 \end{pmatrix} - \begin{pmatrix} 4 \\ 1 \\ 2 \end{pmatrix}$</p> <p>$= \begin{pmatrix} 8 \\ -5 \\ -10 \end{pmatrix}$</p>	<p>M1</p> <p>A1</p> <p>A1</p>	<p>Either $\mathbf{F} + 2\mathbf{G} + \mathbf{H} = \mathbf{0}$ or $\mathbf{F} + 2\mathbf{G} = \mathbf{H}$</p> <p>Must see attempt at $\mathbf{H} = -2\mathbf{G} - \mathbf{F}$</p> <p>cao. Vector must be in proper form (penalise only once in the paper).</p>	3
total		7		

Q3, (Jun 2010, Q3)

<p>(i)</p> $\begin{pmatrix} -1 \\ 14 \\ -8 \end{pmatrix} + \begin{pmatrix} 3 \\ -9 \\ 10 \end{pmatrix} + \mathbf{F} = 4 \begin{pmatrix} -1 \\ 2 \\ 4 \end{pmatrix}$ $\mathbf{F} = \begin{pmatrix} -6 \\ 3 \\ 14 \end{pmatrix}$	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>4</p>	<p>N2L. Allow sign errors in applying N2L. Do not condone $\mathbf{F} = m\mathbf{g}\mathbf{a}$. Allow one given force omitted.</p> <p>Attempt to add $\begin{pmatrix} -1 \\ 14 \\ -8 \end{pmatrix}$ and $\begin{pmatrix} 3 \\ -9 \\ 10 \end{pmatrix}$</p> <p>Two components correct cao</p>
<p>(ii)</p> $\mathbf{v} = \begin{pmatrix} -3 \\ 3 \\ 6 \end{pmatrix} + 3 \begin{pmatrix} -1 \\ 2 \\ 4 \end{pmatrix} = \begin{pmatrix} -6 \\ 9 \\ 18 \end{pmatrix} \text{ so } \begin{pmatrix} -6 \\ 9 \\ 18 \end{pmatrix} \text{ m s}^{-1}.$ <p>speed is $\sqrt{(-6)^2 + 9^2 + 18^2} = 21 \text{ m s}^{-1}.$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>F1</p> <p>4</p>	<p>$\mathbf{v} = \mathbf{u} + t\mathbf{a}$ with given \mathbf{u} and \mathbf{a}. Could go via \mathbf{s}. If integration used, require arbitrary constant (need not be evaluated)</p> <p>cao isw</p> <p>Allow -6^2 even if interpreted as -36. Only FT their v.</p> <p>FT their \mathbf{v} only. [Award M1 F1 for 21 seen WWW]</p>
	<p>8</p>	

Q4, (Jun 2011, Q3)

(i)	$-6 = -2 \times 3$ $\text{so } y = 3 \times 3 = 9 \text{ and } z = -4 \times 3 = -12$	<p>M1 A1</p> <p style="text-align: center;">2</p>	<p>May be implied Both correct [Award 2 for both correct answers seen WW]</p>
(ii)	$\begin{pmatrix} -2 \\ 3 \\ -4 \end{pmatrix} + \begin{pmatrix} 3 \\ -5 \\ -1 \end{pmatrix} = 5\mathbf{a}$ $\mathbf{a} = \begin{pmatrix} 0.2 \\ -0.4 \\ -1 \end{pmatrix} \text{ so accn is } \begin{pmatrix} 0.2 \\ -0.4 \\ -1 \end{pmatrix} \text{ m s}^{-2}$ Magnitude is $\sqrt{0.2^2 + (-0.4)^2 + (-1)^2}$ $= 1.09544\dots$ so 1.10 m s^{-2} , (3 s. f.)	<p>M1 B1 A1</p> <p style="text-align: center;">5</p>	<p>Use of Newton's 2nd Law in vector form for all 3 cpts of attempted resultant Treat use of wrong vectors as MR.</p> <p>Correct LHS</p> <p>The acceleration may be written as a magnitude in a given direction.</p> <p>FT their values. Condone missing brackets. Condone no – signs. Accept 1.1. Accept surd form. Must come from a vector with 3 non-zero components for a</p>
		<p style="text-align: center;">7</p>	

Q5, (Jun 2014, Q6)

(i)	$\text{Speed} = \sqrt{(-5)^2 + 0^2 + (-10)^2}$ $= 11.2 \text{ ms}^{-1} \quad (11.18)$ $\tan \theta = \frac{5}{10}$ $\theta = 26.6^\circ$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>For use of Pythagoras. Accept $\sqrt{5^2 + 10^2}$.</p> <p>Accept $\sqrt{125}$ or $5\sqrt{5}$</p> <p>Complete method for correct angle; may use $\sin \theta = \frac{5}{11.2}$, $\cos \theta = \frac{10}{11.2}$.</p> <p>Allow 153.4°, 206.6°</p>	
(ii)	$\begin{pmatrix} 0 \\ 0 \\ -980 \end{pmatrix} \text{ her weight}$ $\begin{pmatrix} 0 \\ 0 \\ 880 \end{pmatrix} \text{ resistance to her vertical motion}$ $\begin{pmatrix} 50 \\ -20 \\ 0 \end{pmatrix} \text{ force from the power unit}$	<p>B1</p> <p>B1</p> <p>B1</p> <p>[3]</p>	<p>The descriptions should be linked to the forces, either by the layout of the answer or by suitable text. If not, assume that the forces they refer to are in the order given here (which is the same as the question).</p> <p>Accept "Air resistance", "Arms stretched out" and similar statements. Condone mention of a parachute.</p>	
(iii)	$\text{Resultant force} = \begin{pmatrix} 50 \\ -20 \\ -100 \end{pmatrix}$ $\text{Acceleration} = \begin{pmatrix} 0.5 \\ -0.2 \\ -1 \end{pmatrix}$ $\text{Magnitude} = \sqrt{0.5^2 + (-0.2)^2 + 1^2} = 1.1357...$ <p>So 1.14 to 3 s.f.</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>[3]</p>	<p>May be implied</p> <p>Newton's 2nd Law</p> <p>Answer given. Allow FT from sign errors. Accept $\mathbf{F} \div 100$</p>	

Q6, (Jun 2013, Q3)

<p>(i)</p>	<p>p $\sqrt{(-1)^2 + (-1)^2 + 5^2} = \sqrt{27}$</p> <p>q $\sqrt{(-1)^2 + (-4)^2 + 2^2} = \sqrt{21}$</p> <p>r $\sqrt{2^2 + 5^2 + 0^2} = \sqrt{29}$</p> <p>Greatest magnitude: r</p>	<p>M1</p> <p>A1</p> <p>[2]</p>	<p>Use of Pythagoras</p> <p>Note Magnitudes are 5.196, 4.583 and 5.385 respectively</p>
<p>(ii)</p>	<p>Weight = $\begin{pmatrix} 0 \\ 0 \\ -4 \end{pmatrix}$</p> <p>p + q + r + weight = $\begin{pmatrix} 0 \\ 0 \\ 3 \end{pmatrix}$</p> <p>0.4a = $\begin{pmatrix} 0 \\ 0 \\ 3 \end{pmatrix}$</p> <p>Magnitude of acceleration is 7.5 m s^{-2}</p> <p>Direction is vertically upwards</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>[4]</p>	<p>Condone $g = 9.8$ giving weight is $\begin{pmatrix} 0 \\ 0 \\ -3.92 \end{pmatrix}$ N. Accept 4↓.</p> <p>$g = 9.8$ gives $\begin{pmatrix} 0 \\ 0 \\ 3.08 \end{pmatrix}$</p> <p>Relevant attempt at Newton's 2nd Law. The total force must be expressed as a vector in some form. For this mark allow the weight to be missing, in the wrong component or to have the wrong sign. Condone mg in place of m for this mark only.</p> <p>CAO apart from using $g = 9.8 \Rightarrow a = 7.7$</p>